



# General aims of the



# Georg Heinze<sup>1</sup> and Willi Sauerbrei<sup>2</sup> for the STRATOS initiative

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# Statistical methodology – Current situation

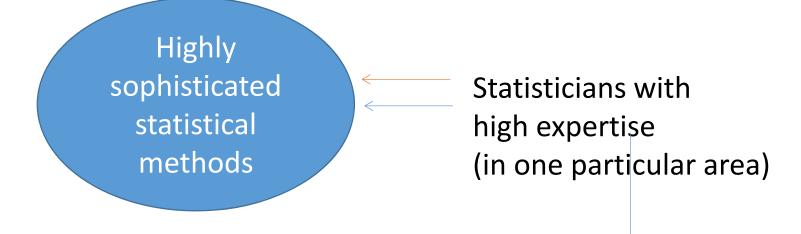
- Substantial development over last decades
- Computer facilities
- Assess properties of complex models using simulation studies
- Resampling and Bayesian methods now easily available
- Wealth of new statistical software packages

Unfortunately, many sensible improvements are ignored in routine analyses





# Why are our improvements ignored?



Analysts with good statistical education

Data analysts with little statistical training





# Why are our improvements ignored?

Highly sophisticated statistical methods, methods

Statisticians with high expertise (in one particular area)

Analysts with good statistical education

Data analysts with little statistical training





# improvements ignored?

Highly sophisticated statistical methods, methods, methods, ...

Statisticians with high expertise (in one particular area)

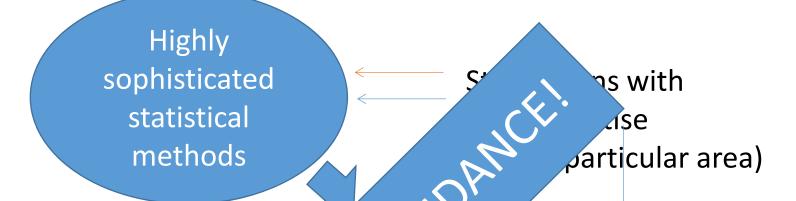
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## STRengthening Analytical Thinking for Observational Studies: the STRATOS initiative

Willi Sauerbrei,<sup>a\*†</sup> Michal Abrahamowicz,<sup>b</sup> Douglas G. Altman,<sup>c</sup> Saskia le Cessie,<sup>d</sup> and<sup>‡</sup> James Carpenter<sup>e</sup> on behalf of the STRATOS initiative

### Statistics in Medicine 2014

2011	ISCB Ottawa, Epidemiology Sub-Comm.	Preliminary ideas
2012	ISCB Bergen	Discussions, SG
2013	ISCB Munich	Initiative launched
2014-16	ISCB	<b>Invited Sessions</b>
2016	Banff	Workshop
2016	IBC Victoria	<b>Invited Session</b>
2016	HEC Munich	<b>Invited Session</b>
2017	IBS-EMR Thessaloniki	<b>Invited Session</b>
2017	CEN-ISBS Vienna	<b>Invited Session</b>

http://www.stratos-initiative.org/

**Basic information** 

c		Topic Group	Chairs and further members				
]			Chairs:	James Carpenter, Kate Lee			
	1	Missing data	Members:	Melanie Bell, Els Goetghebeur, Joe Hogan, Rod Little, Andrea Rotnitzky, Kate Tilling, Ian White			
		<b>Selection of variables</b>	Chairs:	Michal Abrahamowicz, Aris Perperoglou, Willi Sauerbrei			
	2	and functional forms in multivariable analysis	Members:	Heiko Becher, Harald Binder, Frank Harrell, Georg Heinze, Patrick Royston, Matthias Schmid			
	3	Initial data analysis	Chairs:	Marianne Huebner, Saskia le Cessie, Werner Vach			
	3	Initial data analysis	Members:	Maria Blettner, Dianne Cook, Heike Hofmann, Hermann-Josef Huss, Lara Lusa			
		Measurement error and	Chairs:	Laurence Freedman, Victor Kipnis			
	4	misclassification	Members:	Raymond Carroll, Veronika Deffner, Kevin Dodd, Paul Gustafson, Ruth Keogh, Helmut Küchenhoff, Pamela Shaw, Janet Tooze			
			Chairs:	Mitchell Gail			
	5	Study design	Members:	Doug Altman, Gary Collins, Luc Duchateau, Neil Pearce, Peggy Sekula, Elizabeth Williamson, Mark Woodward			
		<b>Evaluating diagnostic</b>	Chairs:	Gary Collins, Carl Moons, Ewout Steyerberg			
	6	tests and prediction models	Members:	Patrick Bossuyt, Petra Macaskill, Ben van Calster, Andrew Vickers			
			Chairs:	Els Goetghebeur			
	7	Causal inference	Members:	Bianca De Stavola, Saskia le Cessie, Niels Keiding, Erica Moodie, Ingeborg Waernbaum, Michael Wallace			
	8	Survival analysis	Chairs:	Michal Abrahamowicz, Per Kragh Andersen, Terry Therneau			
	O	Survival analysis	Members:	Richard Cook, Pierre Joly, Torben Martinussen, Maja Pohar-Perme, Jeremy Taylor			
			Chairs:	Lisa McShane, Joerg Rahnenfuehrer			
	9	High-dimensional data	Members:	Axel Benner, Harald Binder, Anne-Laure Boulesteix, Tomasz Burzykowski, W. Evan Johnson,			



## **Cross-cutting panels**



	Panels	Chairs
1	Glossary (GP)	Simon Day, Marianne Huebner, Jim Slattery
2	Data Sets (DP)	Saskia Le Cessie, Aris Perperoglou, Hermann Huss
3	Publications (PP)	Stephen Walter
3	rublications (FF)	Co- Chairs: Bianca De Stavola, Mitchell Gail, Petra Macaskill
4	New Membership (MP)	James Carpenter, Willi Sauerbrei
5	Website (WP)	Joerg Rahnenfuehrer, Willi Sauerbrei
6	Literature Review (RP)	Gary Collins, Carl Moons
7	Simulation Studies (SP)	Michal Abrahamowicz, Harald Binder
8	Contact with Other Societies and Organizations (OP)	Willi Sauerbrei
9	Knowledge Transfer (TP)	Suzanne Cadarette





# Why many researchers misuse variable selection—and how to prevent this

Georg Heinze and Daniela Dunkler for STRATOS Topic Group 2

Medical University of Vienna

CeMSIIS – Section for Clinical Biometrics





# Current practice of variable selection

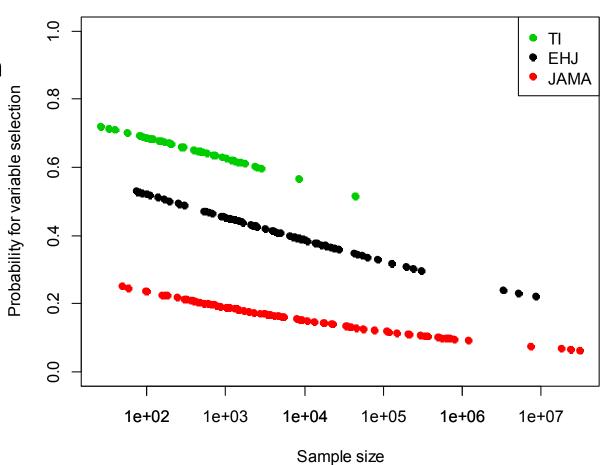
Variable	JAMA Internal Medicine (IF=14.00)	European Heart Journal (IF=15.05)	Transplant International (IF=2.84)
A. Original articles 2015	137	132	89
B. Multivariable models	94	75	49
C. Variable selection (% of B)	17%	37%	65%
Univariate selection (% of B)	5%	21%	39%
Stepwise methods (% of B)	13%	23%	33%
Univariate filtering, then stepwise selection (% of B)	3%	8%	6%
Stability evaluation	0	0	0
Median sample size (in B)	4,396	4,319	295





# Current practice of variable selection

 Modeling the probability for variable selection by journal and sample size:







# The 5 myths about variable selection

- 1. The number of variables in a model should be reduced until there are 10 events per variable.
- 2. Only variables with proven univariable-model significance should be included in a multivariable model.
- 3. Non-significant effects should be eliminated from a model.
- 4. Selected-model p-values are valid.
- 5. Variable selection simplifies analysis.
- → Probably because of these myths univariate selection is so popular.





### Myth 1: reduce until 10 events per variable

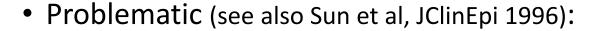
- Often a univariate ,filter' is applied to reduce the variables that are included in a multivariable model
- But this ,filter' is using the outcome data > subject to sampling error
- Ignoring this uncertainty leads to problems
- Better: use only pre-existing knowledge to filter variables

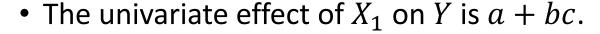


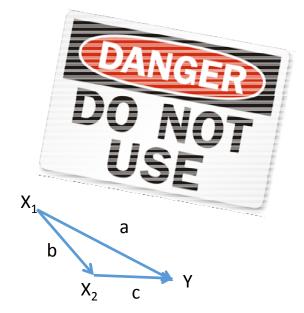


### Myth 2: include only univariately significant variables

- Easy. (You can do that with any software.)
- Retraceable.







a	b	С	Consequence
Pos.	Pos.	Neg.	$X_1$ falsely not selected (if $a = -bc$ )
0	Pos./Neg.	Pos./Neg.	$X_1$ falsely selected.
Pos./neg	0	Pos./neg	$X_1$ correctly selected (only if $b=0$ or $c=0$ ).

→ Univariate selection works only with uncorrelated variables.





## Myth 3: remove non-significant variables

- It is commonly believed that ,non-significant' variables must be removed as they add ,noise' or even ,bias' to the model
- In multivariable analysis, only ABC1 and XYZ2 predicted the outcome.
- Reverse argument: ,X is not selected = X is not a predictor'





### Background knowledge: simple illustrative simulations

• Should X<sub>2</sub> be eliminated from the model?

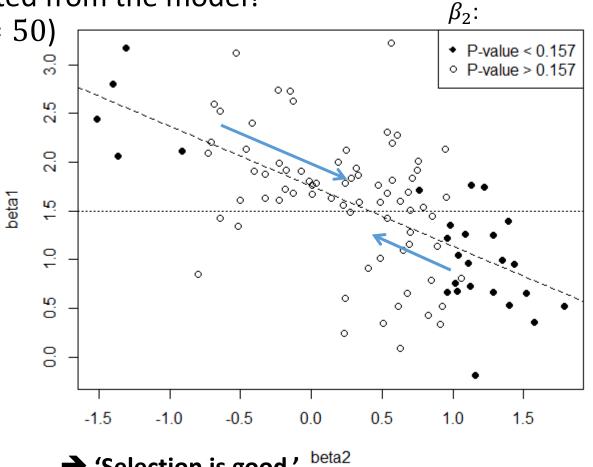
(simulation with N = 50)

True 
$$\beta_1 = 1.5$$
,  $\beta_2 = 0.3$ 

A weak  $\beta_2$ :

Setting it to 0 will more often push  $\hat{\beta}_1$  towards its true value than away from it.

 $\rightarrow$  Shrinkage effect on  $\hat{\beta}_1$ !



→ 'Selection is good.'





### Background knowledge: simple illustrative simulations

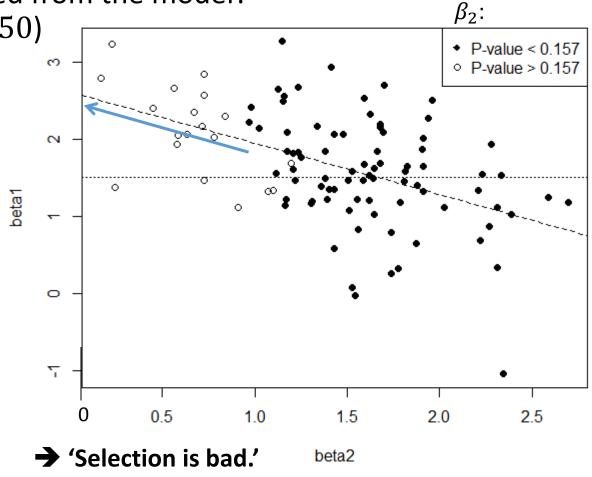
• Should X<sub>2</sub> be eliminated from the model?

(simulation with N = 50)

True 
$$\beta_1 = 1.5$$
,  $\beta_2 = 1.5$ 

A strong  $\beta_2$ :

Setting it to 0 will always push  $\hat{\beta}_1$  away from its true value.







### Myth 4: Selected-model based p-values are valid

- After selection, software routinely reports model based p-values from the finally selected models
- These p-values are grossly misleading (biased low)
- Ignored:
  - uncertainty in selection decisions
  - multiplicity by performing several decisions step-by-step
  - At each step, p-value for  $\beta_i$  tests a different hypothesis!
- Better:
  - For inference, just use the p-values from the full model
  - (you considered all those variables for adjustment!)





### Myth 5: Variable selection simplifies it

- Simple model complex model
- But: additional uncertainty is introduced
- This additional uncertainty should be quantified (Heinze et al, 2017):
  - Selection probabilities of variables
  - Selection probabilities of models
  - Bias conditional on selection
  - RMSD ratios
  - Median coefficient, percentile confidence intervals
- The bootstrap (Sauerbrei and Schumacher, 1992) or subsampling (De Bin et al, 2015) can be used for this





# The 5 myths: and what should change

1. The number of variables in a model should be reduced until there are 10 events per variable.

Resp: No, there should be >>10 events per candidate variable.

2. Only variables with proven univariable-model significance should be included in a multivariable model.

Resp: No, univariable-model significance can be strongly misleading as criterion for inclusion in a multivariable model.

3. Non-significant effects should be eliminated from a model.

Resp: No, non-significant effects do not harm a model.

4. Selected-model based p-values are valid.

Resp: No, P-values after model selection are almost impossible to estimate.

5. Variable selection simplifies analysis.

Resp: No, stability investigations are needed and must become part of routine software output.





# An example

Table 4 Body fat study: full model, model selected by backward elimination with a significance level of 0.157 (AIC selection), and some bootstrap-derived quantities useful for assessing model uncertainty.

	Full model		Bootstrap	Selected model		DMCD	Relative	Bootstrap	Bootstrap	Bootstrap
Predictors	Estimate	Standard error	inclusion frequency (%)	Estimate	Standard error	RMSD ratio	conditional bias (%)	median	2.5 <sup>th</sup> percentile	97.5 <sup>th</sup> percentile
(Intercept)	4.14	23.27	100.0	5.95	8.15	1.06		4.27	-48.49	50.40
abdomen	0.90	0.09	100.0	0.87	0.06	1.06	-1.0	0.89	0.69	1.06
wrist	-1.84	0.53	97.5	-1.73	0.48	1.08	-1.5	-1.81	-2.79	-0.61
age	0.07	0.03	84.6	0.06	0.02	1.14	+5.2	0.07	0.00	0.13
height	-0.11	0.07	68.4	-0.13	0.05	1.14	+37.4	-0.11	-0.25	0.00
neck	-0.40	0.23	62.4	-0.33	0.22	1.24	+29.8	-0.38	-0.81	0.00
forearm	0.28	0.21	55.3	0.36	0.19	1.13	+46.4	0.28	0.00	0.64
thigh	0.17	0.15	49.7			1.14	+67.0	0.00	0.00	0.48
chest	-0.13	0.11	49.4	-0.14	0.09	1.14	+66.0	0.00	-0.34	0.00
biceps	0.17	0.17	43.8			1.15	+100.9	0.00	0.00	0.54
hip	-0.15	0.14	40.7			1.09	+86.7	0.00	-0.43	0.00
ankle	0.18	0.22	34.2			1.11	+84.2	0.00	-0.37	0.60
weight	-0.03	0.15	32.9			1.02	+383.3	0.00	-0.36	0.30
knee	-0.04	0.24	18.8			0.81	+203.2	0.00	-0.51	0.43

RMSD, root mean squared difference.

Johnson, 1996





# An example

Table 4 Body fat study: full model, model selected by backward elimination with a significance level of 0.157 (AIC selection), and some bootstrap-derived

a	uantities	useful	for	assessing	model	uncertainty.

Predictors	Full n	(	Bootstrap inclusion	Selected	(	RMSD	Relative conditional	Bootstrap median	Bootstrap 2.5 <sup>th</sup>	Bootstrap 97.5 <sup>th</sup>
11001010	Estimate	Standard error	frequency (%)	Estimate	Standard error	ratio	bias (%)		percentile	percentile
(Intercept)	4.14	23.27	100,0	5.95	8.15	1.06		4.27	-48.49	50.40
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hip		<b>C</b> 1			•		.1.	0.00	-0.43	0.00
ankle	Dear	' Sottwa	are develoj	pers, pl	ease impl	ement	this:	0.00	-0.37	0.60
weight								0.00	-0.36	0.30
knee	INIS	will nei	p to make	resear	cners ale	r't to ti	ne	0.00	-0.51	0.43
	nroh	lems of	variable s	election	n					
	•				1.					
	Your	s Geor	a and Dani	ea						

RMSD, root me

Johnson, 1996





# References

- Full tutorial 'Variable selection for statistical models: a review and recommendations for the practicing statistician' with additional references: <a href="http://tinyurl.com/variable-selection-talk">http://tinyurl.com/variable-selection-talk</a>
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